DNA damage is one of the mechanisms of mutagenesis. Sequence integrity may be affected by the action of thermal changes, chemical agents, both endogenous and exogenous, and other environmental issues. Abnormally high mutation rates are referred to as genomic instability: a phenomenon closely related to the onset of cancer. Mutant genotypes may be able to confer some kind of selective advantage on subclonal cell populations, leading them to multiply until dominance in a localized tissue environment that later becomes the tumour. Cellular stress, especially that of oxidative and ionic nature, is a recognized trigger for DNA-damaging processes. A physico-chemical model has shown that high hysteresis rates in DNA denaturation curves may be indicative of dissipative processes inducing DNA damage, thus potentially leading to uncontrolled mutagenesis and genome instability. We here study selectively to what extent this phenomenon may occur by analysing the sequence length and composition effects on the thermodynamic behaviour and the presence of hysteresis in pressure-driven DNA denaturation; pronounced hysteresis in the denaturation/renaturation curves may indicate thermal susceptibility to DNA damage. In particular, we consider highly mutated regions of the genome characterized in diffuse large B-cell lymphoma on a recent whole exome next-generation sequencing effort.

1. Introduction

Biophysical approaches are becoming increasingly valuable to understand cancer biology. One important example may be found in the study of DNA damage; the molecular degradation of genomic information due to physico-chemical variations in the DNA molecule. Such variations (mutations) may be produced by a variety of endogenous and exogenous mechanisms [1,2]. By understanding the biophysical mechanisms underlying DNA damage and its associated biochemical consequences, molecular biologists and oncologists may be better equipped to attack the foundations of genome instability that, according to our current understanding, may be behind the ultimate origins of cancer.

In this work, we make use of our recent molecular model for the thermodynamical response of DNA to both ionic stress and temperature variations [3], and we study the thermodynamic effects of ionic stress in some genes that have significant mutation rates, essential for the pathogenesis of diffuse large B-cell lymphoma (DLBCL) [4]. This systematic study allows us to present, for the first time, a hysteresis map that may be associated with stress-induced DNA damage in DLBCL.

The DNA molecule, the ultimate repository of organismal information at the genomic level, is quite susceptible to being damaged. Indeed, the loss of DNA integrity is extremely common: 10 000 DNA lesions occur per cell per day on average [1]. Preserving the integrity of information in DNA is of foremost importance due to the impact it has on processes, such as carcinogenesis, autoimmune diseases, ageing and other common pathologies [5–7]. The information content in the DNA may be damaged by a number of endogenous and exogenous...
causes. The metabolism and function of the cell may produce DNA-damaging elements, such as reactive oxygen species, dehydration and other sources of ionic variations in the cell [5,6]. Environmental causes often include ionizing or UV radiation, extreme thermal variations or poisoning by chemicals known as genotoxic or mutagenic agents [1,7].

Owing to the extreme life-threatening phenomenon that DNA damage may trigger, the cells possess a machinery that when working properly may be able to repair the mutagenic damage caused to DNA. Such processes are generically known as the DNA damage response system [5,7]. The latter is composed of biochemical modules that involve DNA damage recognition; signal transduction processes leading to the activation of cellular responses to either repair DNA locally, rearrange the chromatin structure in a vast portion of DNA or, if the damage is irreparable, promote controlled mechanisms of cell death such as apoptosis [5]. DNA damage is closely related to the onset and development of cancer [2]. Genomic instability caused by mutations leads to functional genomic failure, pathway alteration and systemic disruption [8]. However, DNA damage response systems are also of importance because they are currently one focus of attention in the development of cancer therapeutics [2,9].

It is a known fact that the DNA damage phenomenon is particularly important for the development of DLBCL [10,11] in particular, since many highly susceptible genes, fragile to DNA-damaging agents, are in turn part of the DNA repair machinery [12]. For instance, in [10] the authors report that there is a molecular interaction between the MAP kinase 3 (ERK1/ERK2) complex and CHK2, a protein that plays a central role in the DNA damage checkpoint that responds to DNA double-strand breaks. CHEK2 mutations were first reported in Li-Fraumeni familial syndrome, then the presence of damaged CHEK2 was discovered in a number of sporadic, i.e. non-familial, malignancies and nowadays CHEK2 is considered an important cancer susceptibility gene—though not really a tumour-suppressor gene [10]. Differences in DNA-damaged sites often lead to different gene expression patterns that have proved to be characteristic to different DLBCL molecular subtypes with different associated prognoses [13].

Understanding the physico-chemical origins of DNA damage may thus be an important research problem in relation to pathologies such as DLBCL regarding both its basic and clinical aspects. A simple model for the mechanism may be outlined as follows: certain specific regions in the genome—that may correspond to candidate hypermutation sites—possess sequence-specific features that make them more susceptible to DNA damage by ionic stress. ‘If this is the case, then their corresponding denaturation/renaturation plots may show large hysteresis’. By studying the thermodynamic profiles of specific regions of the genome that are known to be hypermutated in certain pathologies (such as DLBCL), one may gain a better understanding of the mechanisms behind DNA damage and its ultimate molecular causes. The main goal of this work is, thus, to present a map of denaturation/hysteresis in genes associated with DLBCL. This information may allow us to study a possible connection between DNA damage and stress-induced hysteresis.

To close the Introduction, we should point out that the novelty of this work, when compared with our recent work [3], arises from the use of a more realistic DNA model to describe the role of electrostatics on the thermodynamic properties of highly charged DNA suspensions; we have refined the Poisson–Boltzmann (PB) approach to properly account for the main features of the DNA molecule, since in [3] the DNA molecule was assumed to be a very long, almost one-dimensional, and solid cylindrical object whereas in this work we introduce a porous cylinder. Besides, we have also dealt with biological sequences for real genes (both in sequence size and composition). In particular, we here focus on the role of gene length on the hysteresis phenomenon. The rest of the manuscript is outlined as follows: §2 presents the theoretical framework of the methods and models used to study stress-induced DNA denaturation. In §3, we show the results of applying such models to DLBCL hypermutated genes, namely, ACTB, MYD88, BTG1, TP53, KRAS, EZH2, CARD11 and PCLO and discuss some physico-chemical aspects in their response to ionic stress and pressure-driven denaturation that may be relevant to DNA damage. Section 4 deals with some conclusions and perspectives for future work.

2. Material and methods

2.1. Thermodynamics of stress-induced DNA denaturation

The interaction between DNA and the smaller size charged groups, also known as micro-ions, is mainly electrostatic. Its understanding is basic when phenomena, such as denaturation in charged biomolecules, are of particular interest. For instance, at low salinity, the osmotic pressure of a suspension made up of DNA molecules is determined by the electrostatic contribution to the free energy. Thus, any theory that accounts for stress-induced DNA denaturation has to include the electrostatic information during the denaturation process.

Electrostatic interactions between charged biomolecules can be well described by the PB equation [14]. In particular, we use the so-called PB-cell approximation [15]. This framework has successfully been applied to analyse the thermodynamic properties of highly charged colloids in suspension (see, for instance, [16,17] and references therein). We assume that the DNA molecule can be well-represented by a cylindrical-like structure. This is particularly motivated by the fact that experimental measurements of the micro-ion distribution around a DNA molecule agrees well with the cylindrical cell model [18]. Furthermore, this kind of approximation allows us to obtain an analytical expression of the electrostatic potential and, therefore, an analytical representation of the equation of state of DNA molecules in an aqueous-like environment [19,20]. All technical details to solve the PB-cell equation and determine the equation of state are explicitly presented in the electronic supplementary material.

Recently, we have proposed a theoretical framework that describes the process of denaturation of DNA molecules in suspension [3]. This theory makes use of an irreversible thermodynamics approach that is able to predict hysteresis curves for DNA sequences in terms of DNA configurational states, as well as system parameters like salt concentration, density and temperature [3]. Our theoretical framework provides an expression that relates the fraction of broken hydrogen bonds, $\Delta N_H$, with the osmotic pressure, $\Delta \Pi$, and the rate of energy dissipation, $\dot{T}$ (with $T$ and $\dot{T}$ being the absolute temperature and the constant (steady-state) non-equilibrium entropy production [3], respectively), during the denaturation process. In the particular case of a cylindrical-like DNA molecule, the fraction of broken hydrogen bonds reads as follows:

$$\Delta N_H = \frac{\dot{T}T - (\langle 10 cm^3 \rangle / c_{DNA} X A) \Delta \Pi}{(k_B / (10 cm^3)) / (4 \hbar F(T) X A / c_{DNA}) \langle (\langle F_{DNA} \rangle / c_{DNA}) \rangle X A},$$

(2.1)
where \( F(T) = \frac{d\Delta H}{dT} \) is the rate of temperature-broken hydrogen bonds, \( k_B \) is the Boltzmann’s constant, \( l_B \) is Bjerrum’s length, \( N_A \) is Avogadro’s number, \( c_{DNA} \) is the molar concentration of DNA, \( \chi_{DNA} \) is the normalized compressibility and \( V_{DNA} = \pi a^2 l \) is the volume of a cylindrical DNA molecule of length \( l \) and radius \( a \). The quantity \( F(T) \) is a factor that is known both experimentally and from models as the one proposed by Poland & Scheraga [21] and Blake et al. [22]. This factor can also be obtained by the MeltSim algorithm developed and implemented by Blake et al. [22]. MeltSim uses as input both the sequence of DNA and the salt concentration.

As stated above, \( \Delta \phi \) is a phenomenological parameter representing the fraction of broken hydrogen bonds as a function of the thermodynamic state of the system. Such phenomenon can be traced back to eqn 1 of [3]: it is introduced by means of the memory function formalism (eqn (19) therein). The memory kernel introduced there has been found to be compliant with Maxwell–Cattaneo–Vernotte (MCV)-type hyperbolic transport equations typical of extended irreversible thermodynamics. The phenomenological connection is given in terms of response coefficients, via eqn (22) of [3], which relates the changes in this term to the dynamics of uncompensated heat production (akin to entropy production in linear irreversible thermodynamics). Explicit mathematical details of the formal calculation are given in [3] (eqns (22)–(35) therein), as well as in the electronic supplementary material.

\( \Delta \phi \) in DNA denaturation is thermally coupled to other dissipative processes in the system in such a way that we can relate rates of change of the system to changes in the thermodynamic state of the system, most notably with changes in the osmotic pressure. Indeed equation (2.1) can be derived in a straightforward manner from eqn (36) in [3]; however, the model to calculate the effects of the osmotic pressure from the PB formalism (see the electronic supplementary material) is an extended irreversible model of the thermodynamic state of the system. Such phenomenology is described by the model for thermal denaturation. It is explicitly computed using the MeltSim code [22].

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To calculate denaturation curves, one first needs to solve the cylindrical PB-cell equation to connect the electrostatic information with the EOS. From the EOS, we straightforwardly compute the normalized compressibility (see the electronic supplementary material). This information together with the function \( F(T) \) is substituted into equation (2.1) to evaluate the fraction of broken hydrogen bonds. We should recall that the DNA melting temperature dependency enters into our model via the function \( F(T) \), which is computed from a stochastic matrix approach relying on the Poland Scheraga theory of DNA denaturation [21] and implemented in the MELTSIM algorithm [22], a widely used model for thermal denaturation.

To explicitly demonstrate how a denaturation curve exhibits hysteresis, we refer to figure 1, which displays the fraction of broken hydrogen bonds as a function of osmotic pressure. This is done particularly for the \( \text{MEF2B} \) gene, for which hysteresis becomes quite evident. Where \( \Delta \phi = 0 \) is the value of a completely denatured DNA chain and \( \Delta \phi = 1 \) the value of a totally denatured one. We consider the presence of hysteresis due to the fact that for different values of \( T' \) denaturation curves become closer in the extremes, which could indicate a change from the original DNA thermal state so that the gene may be susceptible to damage.

Hysteresis as a non-equilibrium phenomenon is closely related to the presence of dissipative processes affecting the internal structure of molecular systems. Such dissipative processes affect the way such systems respond to environmental conditions. In the present case, the rationale is that genomic sequences that are more prone to be damaged by ionic/osmotic stresses are the ones that will exhibit hysteresis to a greater degree since the denaturation and renaturation processes are far from being the same. Let us recall that in the non-dissipative scenario, denaturation and renaturation processes will be described by a unique equilibrium curve describing an equilibrium phase transition.

### Table 1. Structural features of the B-DNA molecule [26].

<table>
<thead>
<tr>
<th>parameter</th>
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<td>radius</td>
<td>( a )</td>
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<tr>
<td>charge separation</td>
<td>( l_{DNA} )</td>
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<td>linear charge density</td>
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associated with the pathogenesis of DLBCL. These genes are hydrogen bonds, first needs to calculate the composition-dependent thermal mic sequences essential for the pathogenesis of DLBCL, one theoretical paper has just been proved experimentally [32].

The rise of the DNA melting turation curve. The curves represent the fraction of broken hydrogen bonds as Figure 1.

What we present here is evidence that genes that exhibit hysteretic behaviour are indeed more sensible to DNA damage by osmotic/ionic stress-induced mechanisms. Of course, as is often the case in biology, there are exceptions to the rule. In this case, it is not only the base composition of the given DNA that determines its damage-ability but as we showed, also parameters such as the length of the DNA strand.

The relationship between DNA thermal stability and the presence of mutations is not new. In the past, abnormal denaturation profiles have been linked to (and even used to detect) mutations [26,27] in a variety of settings including low-level mutations in cancer [28,29], owing to the fact that genomic instability is related to anomalous melting features. Other cases involving melting analysis to uncover mutations also invoke thermal stability considerations [30].

3. Results and discussion

3.1. Temperature-driven DNA denaturation

When talking about DNA melting in dense assemblies, one can find useful the work addressed in [31], where the importance of the (homologous versus random) DNA sequence is discussed explicitly. The rise of the DNA melting temperature due to electrostatic interactions predicted in such a theoretical paper has just been proved experimentally [32].

In order to characterize DNA damage in a number of genomic sequences essential for the pathogenesis of DLBCL, one first needs to calculate the composition-dependent thermal denaturation function, i.e. the rate of temperature-broken hydrogen bonds, \( F(T) \), included in equation (2.1), to study the thermodynamic effects of ionic stress. For the explicit calculation of the factor \( F(T) \), we explore the damage in eight genes associated with the pathogenesis of DLBCL. These genes are \( ACTB, MYD88, BTG1, TP53, KRAS, EZH2, CARD11 \) and \( PCLO \). They were chosen since they presented consistent mutations in DLBCL [4]. To calculate \( F(T) \), we used the program MeltSim 1.0 [22]. This platform allows us to study the rate of temperature-broken hydrogen bonds using as input the sequence of the gene, the salt concentration (sodium molarity), the temperature increment and both the starting and the final temperatures.

The temperature dependence of the \( F(T) \) for all the aforementioned genes is displayed in figure 2. The red arrows indicate the temperature values considered in the hysteresis curves shown further below. When comparing, for example, figure 2(a) with (b), one clearly appreciates the important effect that the size of the sequence has on \( F(T) \); for the gene \( ACTB \) with 3454 bp the maximum peak is around 0.45, while the gene \( PCLO \) with 408 877 bp the maximum peak is 0.121. These differences indicate the strong dependence of \( F(T) \) with the gene size.

Melting curves were calculated for a fixed sodium molarity \( C_{Na} = 0.005 \text{ M} \), to comply with the MeltSim requirement of non-zero salt concentration. This low sodium concentration value does not modify significantly the electrostatic contribution due to the counterions. However, a higher concentration increases the osmotic pressure which provides greater stability to the configuration of the DNA molecule, requiring a higher temperature to break this configuration. Lower values for \( C_{Na} \) show spikes in the breakage of hydrogen bonds in temperatures below the cell temperature (\( T = 37^\circ \text{C} \)).

3.2. Pressure-driven DNA denaturation

Physico-chemical processes, other than temperature increase, commonly trigger in vivo DNA melting that may potentially lead to mutation. These processes include chemical damage, radiation-enhanced melting and, of course, electrostatic interactions with the local ionic environment. The mutagenic character of chemical DNA damage and radiation has extensively been covered in the DNA biophysics literature. However, the effects of the latter has largely been neglected up to this day, with the exceptions of the studies of Cherstvy et al. (see, for instance, [33]) and some previous work from our group.

Abnormal DNA melting processes are known to have potential mutagenic character. Indeed, the role that DNA-damaging agents may have in the onset of cancer (and even in therapeutic interventions) has largely been discussed (see, for instance, [34–39]). Most of the discussion around this issue has been focused on the role that chemical denaturing agents may have in cancer-related mutagenesis. However, as a whole phenomenon, DNA melting sensitivity has been linked to cancer-related mutagenesis for many years now [40,41].

As we already stated, less attention has been paid to the potentially mutagenic effects of stress-induced DNA denaturation. This result is counterintuitive, since there is a large literature account of the role that double- and single-strand breaks in DNA may have in mutagenesis and cancer [29,35–37]. For this reason, we have decided to investigate the possible effects that osmotic pressure-enhanced DNA melting may have on specific regions in the genome (previously associated with abnormal mutation rates) linked to a quite specific common neoplasm (in this case DLBCL), whose mutational landscape has been recently studied in a multi-centric collaborative effort in which one of us participated [4].

Enhanced DNA opening may thus lead to damaged mechanisms of excision repair, not only leading to mutation but also affecting the mechanisms of DNA repair [42] with known carcinogenic effects [43–45].
The denaturation curves for the genes previously discussed are shown in figures 3–5. These curves are calculated via equation (2.1), which depends on $T_G$, the energy dissipation in the process, so we plotted several curves corresponding to different values of the dissipation $T_G$. A higher $T_G$ implies that a lot of energy is being dissipated by the system in a fast process, hence no hysteresis effect is expected. By contrast, lower $T_G$ implies a very slow process with small dissipation so no hysteresis is shown either. Therefore, $T_G$ is a measure of the possibility of hysteric behaviour in the system and consequently is indicative of dissipative processes that may induce DNA damage. To investigate the effect of the size in the profile of denaturation, we study the CARD11 and PCLO genes, which have a sequence size of over 100,000 bp. For the CARD11 gene or regulator of cell death, we show denaturation curves for the conditions already studied (figure 3b). The plots display a considerable rate of hydrogen bonds breaking higher than 75%, and only present a completely denaturated state for a pair value of $T_G$ at $T = 50°C$.

In order to highlight the various degrees of hysteresis present on different molecules, figures 3–5 also display values of the minimum and maximum variance in the $\Delta B_o$ values for the denaturation plots. One should recall that differences in variance may extend over several orders of magnitude, even when $B_o$ is a normalized quantity. The bigger the difference in variance, the higher the effect of hysteresis. Major changes within a single denaturation–renaturation curve imply a higher area in between the curves. This area is thus proportional to the degree of hysteresis and is a monotonic growing function of the energy dissipation rate. Let us also recall that the dependence with the sequence size was discussed previously and accounted in the factor $F(T)$.

Denaturation curves for the PCLO gene are shown in figure 3a. The gene has 408 877 bp and is found on chromosome 7. Studies have revealed that recurrent mutations in this gene

Figure 2. Rate of temperature-broken hydrogen bonds $F(T)$. The melting curves were obtained for the genes: (a) ACTB, (b) MYD88, (c) BTG1, (d) TP53, (e) KRAS, (f) EZH2, (g) CARD11 and (b) PCLO. The red arrows (those with no asterisk) indicate the temperature value used in the calculation of the denaturation curves, and the blue arrows (marked with asterisk (‘*’)) show the physiological temperature. (Online version in colour.)
have been associated with cases of DLBCL [4]. The denaturation profile for this gene shows a fully denatured state with the two strands completely separated. From figure 3, it is evident that CARD11 exhibits hysteretic behaviour at $T = 50\, ^\circ\mathrm{C}$. And the same behaviour is shown for the PCLO gene at $T = 40\, ^\circ\mathrm{C}$. As already discussed, the hysteresis presence in this curve may be evidence of possible DNA damage under these conditions.

As we mentioned earlier, there is a potential relation with the phenomenon of stress-induced DNA damage that has been related to cellular ageing and disease effects [46]. In the particular case of the MYD88 gene (results for this gene will be presented later), there is proof that the deficiency of this gene affects the immune system and may cause a null response of the body to produce a defence mechanism against disease [47]. Moreover, in several studies, MYD88 has been found mutated in several patients with DLBCL [4,48]. In figure 3, we present the denaturation curves for the *human enhancer of zeste 2* or *EZH2*, a gene implicated in the progression of various types of human cancers [49]. Recurrent *EZH2* mutations have been identified in B-cell lymphomas [4]. The hysteretic behaviour at a temperature of $40\, ^\circ\mathrm{C}$ is displayed in figure 3c. For this condition, DNA shows a completely denatured state. However, when the temperature increases to $T = 50\, ^\circ\mathrm{C}$ a rate of bond breaking less than 50% is exhibited.

One of the most important genes in cancer genetics is the *TP53* gene. The tumour-suppressor protein p53 is essential for regulating cell division and preventing tumour formation, reasons why it is nicknamed *guardian of the genome*. Diverse studies have demonstrated that *TP53* presents mutations in more than 50% of all types of human cancer, since it is encoded in a multifunctional protein whose absence contributes to genomic instability [50,51]. We studied the denaturation profile for *TP53* in figure 4. In the same way as in previous figures, the curves show a strong temperature dependence, which is related to the number of broken hydrogen bonds within the molecule. In both cases ((a) $T = 40\, ^\circ\mathrm{C}$ and (b) $50\, ^\circ\mathrm{C}$), the gene is found in a completely denatured state, moreover, the plots present in its extremes a closer path for the different dissipation rates enabling the identification of hysteretic behaviour for these conditions.

In figure 4, we present the denaturation map for (c) *BTG1*, and (d) *KRAS* at $T = 40\, ^\circ\mathrm{C}$ and $37\, ^\circ\mathrm{C}$, respectively. The conditions chosen are such that the curves show complete denaturation. One can appreciate that *KRAS* presents possible damage at cell temperature, a product of the coupling between temperature and pressure in the denaturation process. *KRAS* damage is one important triggering mechanism for genomic instability. Among other things, this has led to *KRAS* being defined as an oncogene.

Finally, we show the results in figure 5 for the *ACTB* and *MYD88* genes. *ACTB* (*Actini Beta*) is located on chromosome 7. This gene provides instructions for making the protein called $\beta$-actin, which plays important roles in determining cell shape and controlling cell movement. Moreover, the mutation in this gene has been identified in some patients with DLBCL and Baraitser–Winter syndrome, a well-defined disorder characterized by distinct craniofacial features [4,52]. Even when the *ACTB* gene is found mutated in some cases,
minimum and maximum variances, respectively. (Online version in colour.)

Figure 4. Denaturation curves as a function of temperature and osmotic pressure for the TP53 gene. (a) $T = 40^\circ C$ and (b) $T = 50^\circ C$. And also for the (c) KRAS and (d) BTG1 genes. These curves are plotted for conditions that allow 100% of broken bonds. $\sigma_{\text{min}}$ and $\sigma_{\text{max}}$ denote the minimum and maximum variances, respectively. (Online version in colour.)

Figure 5. Denaturation curves as a function of temperature and osmotic pressure for the (a) ACTB and (b) MYD88 genes. $\sigma_{\text{min}}$ and $\sigma_{\text{max}}$ denote the minimum and maximum variances, respectively. (Online version in colour.)

Figure 5a does not show conclusive evidence of hysteresis in the denaturation curves, however, this does not imply that under other conditions of temperature and concentration it could not show hysteretic behaviour. By contrast, we can consider the denaturation curves given in figure 5b for the myeloid differentiation primary response gene 88, also known as MYD88 gene. In this scenario, for the same denaturing conditions as the previous case, it is possible to observe that, under the same dissipation rate $TT$ the behaviour is distinct; we see the difference in the form of the curves, in figure 5a for the ACTB gene (for which the fully denatured state is not present), and for the MYD88 gene. In figure 5b, one sees that the denaturation occurs so rapidly that we cannot see whether there is hysteresis or not. It is important to mention that, although under these conditions neither of the ACTB and MYD88 genes showed hysteresis in the denaturation curves, if we change the conditions of the system, such as the sodium concentration, the value of $F(T)$ changes and in turn, the coupling between temperature and osmotic pressure also changes giving, as a possible result, very clear hysteresis. These results are not shown here due to the fact that we are working in the no added salt regime.

4. Conclusion

In this work, we have considered hysteresis in the denaturation curve for specific genes (in particular, some genes that are known to be mutated in DLBCL) as indicative of possible
DNA damage. To measure the denaturation extent of a gene, we have used, on the one hand, a mean field theory that describes the distribution of counterions around a porous, negatively charged cylinder (the DNA model), and, on the other hand, an irreversible thermodynamics framework to measure the fraction of broken hydrogen bonds due to the coupling between the temperature and osmotic pressure. An observation of the results just presented is the important role that sequence length has on the hysteretic behaviour. The first genes displayed in the Results and discussion are the larger ones, and clearly show hysteresis in the curves. On the contrary, the last genes are the shorter ones and do not show this behaviour. In this context, the results presented for the KRAS gene seem to be quite significant, because the curve exhibits hysteresis even at physiological temperature, which could indicate a higher probability of DNA damage. Changes in the structure of the DNA depend on the energetic interactions between DNA and proteins. The results presented here, where the counterions are removed, clear show this behaviour. In this context, the results presented for the KRAS gene seem to be quite significant, because the curve exhibits hysteresis even at physiological temperature, which could indicate a higher probability of DNA damage. Changes in the structure of KRAS have, of course, been closely related with the onset of cancer.

We also considered the denaturation of DNA sequences under no-salt conditions. Clearly, this situation does not correspond to a real physico-chemical condition, but allows us to build, for the first time, a hysteresis map that might shed light on the possible damage that occurs in DNA. Furthermore, this case pointed towards the importance of the contribution of counterions to the phenomenon of hysteresis observed during driven-pressure DNA denaturation. The effect of salt is a topic that deserves further investigation, since such an effect might lead to a more clearly hysteretic behaviour in gene sequences.

We should point out that in this work we have implemented a more realistic DNA model (see the electronic supplementary material) and used real gene sequences. As a direct result, we emphasized the importance of sequence length on the hysteresis phenomenon. This result is similar to previous published work [31,32], where the relevance of the sequence is key when studying DNA melting.

Our results might be partially corroborated through time-consuming computer simulations using a coarse-grained model for the DNA structure. In particular, it would be rather interesting to use such a computational approach to investigate, for example, the impact on the mechanisms of hysteresis due to the B–Z DNA transition driven by salt concentration [53]. In fact, in order to reach physiological conditions, i.e. high salt concentrations, one should use a combination of computer simulations and statistical analyses to explore the thermodynamic properties of DNA melting [53,54]. Thus, more realistic models, supplemented with detailed spectroscopic [55] and calorimetric experimental data at the mesoscopic level (to date almost non-existent but foreseeable in the near future) may surely lead to a refinement of our results. In addition, incorporating other sources of chemical and physical DNA damage (for instance, oxidative stress and not only ionic stress) will be of foremost importance. All in all, there is still a lot of work to do to have a relatively complete understanding of the molecular mechanisms of DNA damage as well as its relation to oncogenic processes.

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