Biomechanics and control of vocalization in a non-songbird

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The neuromuscular control of vocalization in birds requires complicated and precisely coordinated motor control of the vocal organ (i.e. the syrinx), the respiratory system and upper vocal tract. The biomechanics of the syrinx is very complex and not well understood. In this paper, we aim to unravel the contribution of different control parameters in the coo of the ring dove (Streptopelia risoria) at the syrinx level. We designed and implemented a quantitative biomechanical syrinx model that is driven by physiological control parameters and includes a muscle model. Our simple nonlinear model reproduces the coo, including the inspiratory note, with remarkable accuracy and suggests that harmonic content of song can be controlled by the geometry and rest position of the syrinx. Furthermore, by systematically switching off the control parameters, we demonstrate how they affect amplitude and frequency modulations and generate new experimentally testable hypotheses. Our model suggests that independent control of amplitude and frequency seems not to be possible with the simple syringeal morphology of the ring dove. We speculate that songbirds evolved a syrinx design that uncouples the control of different sound parameters and allows for independent control. This evolutionary key innovation provides an additional explanation for the rapid diversification and speciation of the songbirds.

Keywords: birdsong; vocal learning; biomechanics; nonlinear dynamics

1. INTRODUCTION

The neuromuscular control of vocalization in birds requires complicated and well-orchestrated motor control of the vocal organ (i.e. the syrinx), the respiratory system and upper vocal tract. The biomechanics of the syrinx is very complex and not well understood. In this paper, we aim to unravel the contribution of different control parameters in the coo of the ring dove (Streptopelia risoria) at the syrinx level. We designed and implemented a quantitative biomechanical syrinx model that is driven by physiological control parameters and includes a muscle model. Our simple nonlinear model reproduces the coo, including the inspiratory note, with remarkable accuracy and suggests that harmonic content of song can be controlled by the geometry and rest position of the syrinx. Furthermore, by systematically switching off the control parameters, we demonstrate how they affect amplitude and frequency modulations and generate new experimentally testable hypotheses. Our model suggests that independent control of amplitude and frequency seems not to be possible with the simple syringeal morphology of the ring dove. We speculate that songbirds evolved a syrinx design that uncouples the control of different sound parameters and allows for independent control. This evolutionary key innovation provides an additional explanation for the rapid diversification and speciation of the songbirds.

In pigeons, sound is produced in the syrinx by flow-induced oscillations of membranes (Goller & Larsen 1997; Larsen & Goller 1999). The control of the fundamental frequency of the sound and the gating of sound elements happen at the level of the syrinx (Greenewalt 1968; Goller & Suthers 1996a, b). Despite the seeming simplicity of the dove coo, the syrinx demonstrates surprisingly complex dynamics; sound is produced during expiration and inspiration (Gaunt et al. 1982) and the coo exhibits fast trills (Elemans et al. 2004) and frequency jumps (Beckers et al. 2003a).

Many forces act on the sound-producing lateral tympaniform membranes (LTMs; figure 1 b): pressure gradients (Gaunt et al. 1982; Beckers et al. 2003a) and syringeal muscles (Elemans et al. 2004, 2006) affect variations in geometry and tension (Gaunt 1983). These forces affect the tension in the LTM (Gaunt 1983; Fletcher 1992), and most likely also the oscillation amplitude and phonation onsets. This complex interplay of forces is hard to dissect without a quantitative biomechanical approach.

In order to provide a clear overview, it is essential to define some terms on the concepts of modelling. A conceptual biomechanical model is a construct based on physical principles without mathematical analysis.

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A mathematical model is a mathematical construct, which describes some mathematical aspects of the system under study. Basic mathematical models are sometimes referred to as ‘toy models’ or ‘normal forms’. A quantitative (or numerical) biomechanical model is the implementation of a mathematical model in a computer program with which simulations can be made for a selected range of values of the input parameters.

Several conceptual models have been proposed to explain the biomechanics of sound production that uses a separation of single physiological correlates with frequency modulation (FM) and amplitude modulation (AM; e.g., songbirds: Goller & Suthers 1996a,b; doves: Beckers et al. 2003a). This separation in functional attributes is most likely a too simple representation. Especially nonlinear oscillators, which are used to mathematically model syringeal vibrations

Figure 1. Syrinx morphology. (a) Toto view of ring dove syrinx. (b) Longitudinal cross section of ring dove syrinx. Several forces acting on the LVMs: a pressure gradient from bronchus to trachea (red to yellow circles), the transmural pressure $p_t$ from air sac to syringeal lumen (black arrow) and muscle activity (white arrow). (c) Micro-CT scan of the syrinx. Note that, due to its flattened shape, ring T2 is able to better withstand the torques generated by the $m. \text{tracheolateralis}$ (TL). (d) Sagittal cross section through a fresh syrinx slightly below the TL insertion. The right LVM is cut higher, some TL fibres are cut. The arrows indicate LVM width and length as presented in table 1. ICAS, interclavicular air sac; LVM, lateral vibratory mass; $p_t$, transmural pressure; T1–2, tracheal rings; TL, $m. \text{tracheolateralis}$; ST, $m. \text{sternotrachealis}$. The syrinx in (a) has been published in a different form as electronic supplementary material accompanying Elemans et al. (2004) and in Elemans et al. (2006). The syrinx cross section in (b) is modified from Zaccarelli et al. (2006). (see also Alexander 2003).
Over the last decades, the mechanics and physiology of phonation in doves have received some attention, but some data have been interpreted in an older framework that is missing recent insights (e.g. based on the assumption that other structures acted as the principal sound sources). Here, we aim to integrate all observations into a new framework.

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closed and the air is collected in an inflating oesophageal crop (Riede et al. 2004). Direct observations of the syrinx during induced phonation using brain stimuli in pigeons by Goller & Larsen (1997) show that (i) the LTM are the sources of the sound and (ii) the syrinx is brought into a ‘phonatory position’ by two paired syringeal muscles, the musculus sternotrachealis (ST) and musculus tracheolateralis (TL) as hypothesized earlier by Gaunt et al. (1982). Whereas the TL directly affects position in the LTM (figure 1a,b), the ST moves the entire syrinx downward (Goller & Larsen 1997). However, the LTM in ring doves are not thin membranes (see §5), but more resemble labia with larger masses. Therefore, the denomination membrane seems not appropriate and we will argue that lateral vibratory mass (LVM, figure 1) is a more appropriate name than LTM. To avoid confusion, we will consistently use the abbreviation LVM from now on.

Although there are no direct observations in freely singing doves, several indirect measurements support the idea that the syringeal aperture is modulated and controlled by syringeal muscles. First, the duration of TL muscle activity is equal to the duration of sound elements during the trill (Elemans et al. 2004). Second, simultaneous pressure and flow recordings suggest that the syrinx is open during sound production and mostly closed in between sound elements: when sound starts, the bronchial pressure drops and when sound stops flow decreases to almost zero (Gaunt et al. 1982; Beckers et al. 2003a). These observations can be explained by the hypothesis that TL contraction modulates the position of the LVM and as such the syringeal aperture (Elemans et al. 2004, 2006).

After the initial pressure drop due to opening of the syrinx, the bronchial pressure increases again during every sound element in the trill (figure 2a). Gaunt et al. (1982) suggest that this is due to increased activity of the abdominal muscles synchronized with the TL. Indeed, the pressure slope starts increasing at the inflexion points on the negative slope of the pressure curve (figure 2a–c, local minima of dp/dt in figure 2b), which can be indicative of a start of force generation by the abdominal muscles. We measured the delays between abdominal muscle electromyogram (EMG) activity and pressure by digitizing the data presented in Gaunt et al. (1982). The delay between the onset of abdominal muscle EMG activity and the local minima in dp/dt measures 7.7 ± 2.6 ms for the last five trills (figure 2). The pressure starts increasing 21.0 ± 7.4 ms after the onset of EMG activity. These delays are consistent with a typical delay between electrical activity (EMG) and mechanical muscle action for skeletal muscle (e.g. Norman & Komi 1979; Komi 2000; Carroll & Wainwright 2006) and therefore the claim by Gaunt et al. (1982) is feasible. This again emphasizes that the generation of trills in doves demands a high level of synchronization of syringeal and respiratory muscle activation.

The parameters controlling the fundamental frequency are not well established. The common and most simple assumption is that the fundamental frequency (f0) of LVM oscillation is determined by tension in the LVM (Fletcher 1992). Beckers et al. (2003a) report that the f0 correlates with the pressure in the air sac in which the syrinx is suspended; the interclavicular air sac (ICAS). Birds have a unique and elaborate air sac system for respiratory ventilation (Duncker 1971). Pressure differences between air sacs have been reported during many activities, such as normal respiration (Brackenbury 1972), sound production (Brackenbury 1972) and locomotion (Boggs et al. 1998, 2001). Beckers et al. (2003a) hypothesize that ICAS pressure modulates the tension in the LVM. However, tension in the membrane is the result of the net force that acts on the membrane. When looking at the forces acting on the LVM (figure 1b), it becomes clear that any pressure differences between the air sac surrounding the syrinx (the ICAS) and the syringeal lumen causes a net force to act on the LVM. This so-called transmural pressure pt affects the tension in the membrane (Bertram & Pedley 1982; Bertram 2004). We define the transmural pressure as external pressure minus upstream pressure, where we take ICAS pressure as external pressure and assume that the pressure in the caudal thoracic air sac (CTAS) equals upstream or bronchial pressure (see §3.1).

\[
pt = p_{\text{ICAS}} - p_{\text{CTAS}},
\]

where \( p_{\text{ICAS}} \) and \( p_{\text{CTAS}} \) are the pressures in the ICAS and CTAS, respectively. When we derive \( pt \) from the data presented by Beckers et al. (2003a), we see that the calculated \( pt \) is in phase with the pressure in the ICAS (\( p_{\text{ICAS}} \); figure 2d–f). Therefore, correlation techniques cannot differentiate between \( p_{\text{ICAS}} \) and \( pt \) as modulators and as such the function ‘frequency modulator’ cannot be attributed to either one of them using correlation. Considering the mechanics, the LVM tension is affected by both (i) the transmural stress caused by a pressure differential between the bronchus and ICAS and (ii) the stress exerted by muscles.

To summarize, we hypothesize that (i) the tracheolateralis muscle (TL) modulates the position of the LVM and as such the syringeal aperture and (ii) both the transmural pressure and TL stress affect tension in the LVM.

3. COMPILATION OF STANDARDIZED COO

We compiled a quantitative dataset of all the parameters affecting sound production at the syrinx level. Many doves have three different coo types; the nest, bow and perch coo (Goodwin 1983). We did not differentiate between these coos because in ring doves there are no apparent differences in overall acoustic structure (Beckers et al. 2003a). We combined published and additionally collected physiological and morphological data to construct a ‘standard coo’ (figure 3). Our primary focus is the trill where the fastest and most complex interactions occur. If we look at the forces acting on the syrinx membranes (figure 1b), the most important physiological control parameters are (i) the bronchial–tracheal pressure gradient, (ii) the transmural pressure difference and (iii) the stress exerted by syringeal muscles. It should be noted that all these control parameters are the ultimate result of muscle action and therefore all under direct
neural control. All pressures mentioned are gauge pressures, i.e. pressure relative to atmospheric pressure. To construct all synchronized time-dependent parameters of the standard coo, we start with simultaneously recorded signals of emitted sound, CTAS pressure and EMGs of the syringeal muscles. These signals were recorded as part of previous studies (Elemans et al. 2004, 2006). These experiments were in accordance with the Institutional Animal Care and Use Committee (IACUC) of the University of Utah, Salt Lake City, USA.

3.1. The bronchial–tracheal pressure gradient

To understand the vibrations of the lateral vibratory membrane (LVM), we need to know upstream (i.e. bronchial) and downstream (i.e. tracheal) pressures because the pressure drop along the LVM defines the oscillation regime, analogous to collapsible tube systems (e.g. Bertram 2004; Groberg & Jensen 2004) and human vocal fold models (Titze 2002).

To estimate upstream pressure, i.e. the bronchial pressure, the common assumption is that pressure in two easily accessible air sacs, either the pressure in the posterior thoracic air sac (PTAS) or CTAS, equals bronchial pressure for most species of birds (e.g. Gaunt et al. 1982; Suthers et al. 1994; Goller & Suthers 1996a; Mindlin et al. 2003; Suthers & Zollinger 2004). To our knowledge, no record of direct bronchial pressure exists of any bird species during song. We studied silicone casts of the air sac system in ring doves and found that the connections or ostia of the CTAS are close to the bronchi (1–3 mm), cf. Duncker (1971). Therefore, also in this case, it is safe to assume that the pressure in the CTAS is a good estimate for bronchial or subsyringeal pressure.

Published PTAS and CTAS pressure patterns for ring doves are highly similar (compare PTAS pressure in figs 5–7 in Gaunt et al. (1982) with CTAS pressure in figs 1 and 2 in Beckers et al. (2003a) and CTAS pressure in figure 3b in this paper). A small phase shift between the pressure waveforms of air sacs cannot be ruled out, but from what is known from morphology and airflow pattern models there is no reason to assume large differences in amplitude (Brackenbury 1972). We assume that no phase shift is introduced in the measurements due to the time constant of the technique to measure pressure in air sacs (i.e. an extracorporeal sensor with a short cannula to the air sac).

The maximal pressure in the PTAS and CTAS is 3.5 kPa (equal to 35 cmH₂O), with a slight variation introduced by the emotional state of the individual bird (Gaunt et al. 1982). Therefore, it is reasonable to set the maximal pressure for CTAS, PTAS and ICAS in the air sac system to 3.5 kPa. To determine the bronchial–tracheal gradient, we measured CTAS pressure by cannulating CTAS in six male doves (data collected in collaboration with Dr F. Goller as part of previous studies; Elemans et al. 2004). Our results are consistent with earlier measurements; maximal pressure is 3.5 kPa and the temporal pattern is highly similar (figure 3b).

Tracheal pressure gradually increases during the coo, because the air is not exhaled but collected in the oesophagus (Gaunt et al. 1982; Riede et al. 2004). The peak pressure for tracheal pressure rarely exceeds 0.5 kPa (equal to 5 cmH₂O) and often only slightly exceeds the respiratory exhalation pressure of 0.1 kPa (equal to 1 cmH₂O). Because this pressure is low compared with the bronchial pressure, we will assume that the downstream pressure equals atmospheric pressure (0 kPa). This simplification implies that the CTAS pressure defines the bronchial–tracheal pressure gradient.

3.2. The transmural pressure differential

As discussed above, any pressure difference between the bronchial–tracheal gradient on one hand and the pressure in the ICAS on the other results in a net force on the LVM and therefore in a tension change in the membrane. As can be seen in figure 2ef, the transmural pressure (p̅t) oscillates in phase with p̅ICAS and almost in phase with p̅CTAS. To reconstruct p̅t from p̅CTAS, we retained the oscillation in p̅CTAS and normalized the magnitude to 1 kPa as measured in figure 2f (bottom trace in figure 3c).

3.3. Syringeal muscles

In ring doves, two syringeal muscles affect LVM position: the paired m. tracheolateralis (TL) and m. sternotrachealis (ST; figure 1). Although the ST seems important for stability of the syrinx (crows: Chamberlain et al. 1968; thrashers: Goller & Suthers 1996a,b; doves: Elemans et al. 2006), they do not act directly on the LVM and we will ignore them here to simplify matters. We use the following algorithm to reconstruct the stress exerted by the TL. First, we define blocks of muscle on/off activity by creating a binary on/off signal from the measured EMG signal (figure 3c). The threshold needed to calculate the binary signal was set to the mean value of the noise level plus three times the standard deviation. Second, we fit exponential rise and fall curves through the tetanic isometric contraction data of Elemans et al. (2004) and calculate their time constants. The maximal stress is set to 20 kN m⁻² (equal to maximal isometric stress from Elemans et al. 2004). Third, we numerically construct the stress signal using the extracted time constants and the on/off EMG signal (figure 3d). We omit the pre-trill pulses of muscle activation (figure 3c) and include only pulses associated with sound elements. The total stress acting on the LVM is \( p_{\text{sum}} = p_{\text{TL}} + p_{\text{ICAS}} \) (figure 3e).

3.4. Morphology

The thickness of the LVM varies along the syrinx. We assume that action of the TL mostly affects the mass between tracheal rings T1 and T2 (figure 1b), because the tracheal rings T2–T20 form a stiff box and both T1 and T2 are flattened rostrocaudally (figure 1c). Furthermore, endoscopic observations by Goller & Larsen (1997) show that, in the rock pigeon (Columba livia), action of TL and ST especially affects the position and tension of the LVM between T1 and T2. We measured the dimensions and estimated mass of the LVM in four adult male ring doves. LVM height is measured between T1 and T2 (figure 1b), and LVM length and width are measured slightly below the TL.
insertion between tracheal rings T1 and T2 (figure 1d) using a MicroPhot-FXA microscope (NIKON) and ANALYSISPro software. These experiments were approved by the Committee of Experimental Animal Use of Wageningen University, The Netherlands.

### 4. BIOMECHANICAL MODEL DESCRIPTION

We modelled one unilateral LVM with two masses and three massless plates adapted to syrinx geometry (based on *Loos et al.* (1998), *Sciamarella & d’Alessandro* (2004) and *Zaccarelli et al.* (2003)) without tracheal filtering. Because two-mass models have been studied intensively for human and non-human phonations, they provide a well-established starting point. Now we contrast our approach to two previously developed types of mathematical syrinx models (for a review of syrinx models, see *Elemans et al.* (1998), *Sciamarella & d’Alessandro* (2004) and *Laje et al.* (2002)) without tracheal filtering.

Figure 4 shows cartoons of our biomechanical syrinx model in three different configurations: convergent, rectangular and divergent. The pressure in the syringleal lumen generates a force on the plates (\( p_{1,2,3} \)) and pushes the masses (\( m_1, m_2 \)) outward, loading the two dampers (\( r_1, r_2 \)) and springs (\( k_1, k_2 \)). The two masses are interconnected by a single spring with coupling constant \( k_c \). Above a threshold value, the subsyringeal pressure induces self-sustained oscillations of the masses. The opening and closing of the syringeal aperture creates pressure waves, i.e. sound.

Following classic two-mass models for human sound production, we obtained the pressures within the syringeal lumen that act directly on the labia using Bernoulli’s law and the jet separation assumption. Bernoulli’s law states that for a fluid confined in a duct or pipe at any point \( x \) along the duct

\[
P + \rho \frac{U^2}{2} = C,
\]

where \( A_x \) is the cross-sectional area of the duct at point \( x \); \( U \) is the flow; \( P \) is the pressure; \( \rho \) is the fluid density; and \( C \) is a constant. Equation (4.1) is used to derive the
mean intraglottal pressure ($P_{in}$) acting on the folds in humans, where the airflow passes through the narrower constriction of the glottis. This expression, assuming no vocal fold collision, idealized flow in the glottis and a supraglottal pressure of 0 leads, in the case of a linear shape, to (Titze 2002 and references therein)

$$P_{in} = P_s \left(1 - \frac{a_2}{a_1}\right),$$ (4.2)

where $P_s$ is the subglottal pressure and $a_1$, $a_2$ are the areas of the glottis at the position of masses $m_1$ and $m_2$ (figure 4c). From equation (4.2), it follows that $P_{in}$ is larger for a convergent shape ($a_2/a_1 > 1$, figure 4a) than for a divergent shape ($a_2/a_1 < 1$, figure 4c). Because the lower mass of the fold moves ahead of the upper mass, outward (lateral) movement is associated with a convergent glottis and inward movement with a divergent glottis. Although equation (4.2) assumes no vocal fold collision, this expression shows how the above process leads to an energy transfer from the flow to the tissue and compensates damping.

We assume that the air stream separates from the vocal fold surface at the smallest syringeal opening area to improve the simulated sound (Pelorson et al. 1994; For the divergent shape, a non-fixed separation point above the jet separation point close to zero. The pressure above the jet separation point decreases when it is opposite to the direction of the labial flow (i.e., labial movement). This means that the driving pressure and labial velocity are in phase, which is an essential mechanism to explain this self-sustained oscillator.

**Table 2. Model parameters.** (For clarification of geometry description, see figure 4.)

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<thead>
<tr>
<th>description</th>
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<td>$L$</td>
<td>3.0</td>
</tr>
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<tr>
<td>rest area of mass 2 (mm$^2$)</td>
<td>$a_0_2$</td>
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* Parameters are rescaled during coo according to equation (4.9).

Our syrinx model deviates from the classical two-mass models in two important points. First, we assume symmetry between the masses ($m_1 = m_2$, $k_1 = k_2$ and $r_1 = r_2$). Second, we introduce a more smooth geometry:

\[
\frac{d^2x_1}{dt^2} = -v_1, \quad \frac{dv_1}{dt} = \frac{1}{m_1} (F_1 - r_1 v_1 - k_1 x_1 + I_1 - k_c (x_1 - x_2)),
\]

on each unilateral side of the LVM the two masses are linked with three massless plates $p_{1,2,3}$ (figure 4a).

We define a collision force $I$ that pushes the two contralateral LVMs away when they collide. The collision force is a linear function of the area where the two LVMs overlap (figure 4b). To evaluate force on each mass, we assume that all forces below the syrinx midline (horizontal line in figure 4b) act on the lower mass $m_1$, whereas all the forces above act on the upper mass $m_2$. Our model is governed by the following equations of motion:
\[ \frac{dx}{dt} = v_x, \quad (4.5) \]
\[ \frac{dv_x}{dt} = \frac{1}{m_2} \left( F_2 - r_2 v_x - k_2 x_2 + I_2 - k_1 (x_2 - x_1) \right), \quad (4.6) \]

where positions \( x_i \) are displacements relative to rest position \( x_0 \); \( F_2 \) are the pressure forces derived from the Bernoulli equation and the jet assumption; and \( I_1 \) represent collision forces. A more detailed description of the equations of motion and pressure evaluation of our model can be found in Zaccarelli et al. (2006). The used tissue properties and geometrical parameters for our default configuration are listed in table 2. The flow derivative \( \dot{U} = (dU)/(dt) \) is used as an approximation of the suprasyringeal sound (Ishizaka & Flanagan 1972).

\[ x_{0i} = \frac{a_{0i}}{2L}, \quad (4.7) \]

where \( L \) is the length of the syringeal base (figure 4c). Using the position \( x_i \) (equations (4.3)–(4.6)) and the rest position \( x_{0i} \) (equation (4.7)), we can consequently calculate the syringeal aperture \( a_i \) at mass \( i \),

\[ a_i = a_{0i} + 2Lx_i = 2L(x_{0i} + x_i). \quad (4.8) \]

We implemented tension modulation of the LVM by means of parameter \( Q(t) \), which redefines the masses and the stiffness of the LVM as a function of time:

\( m(t) = m/Q(t), k(t) = k \cdot Q(t) \), where mass \( m \) and stiffness \( k \) are the default values (table 2). Several implementations of \( Q \) have been used in Ishizaka & Flanagan (1972) and Steinecke & Herzel (1995). The definition of \( Q \) is motivated by the relation \( F_0(t) = (1/2\pi) \sqrt{k/m} \), which defines the natural oscillation frequency \( (F_0) \) of a single mass-spring system. For a detailed analysis of natural frequencies of oscillations of the classical two-mass model, see Titze (2002). The \( F_0 \) as a function of time is

\[ F(t) = \frac{1}{2\pi} \sqrt{\frac{k \cdot Q(t)}{m/Q(t)}} = Q(t) \cdot F_0. \quad (4.9) \]

We systematically explored the bifurcation behaviour of our model using the XPP/XPPAUT0 software package (available at www.math.pitt.edu/~bard/xpp/xpp.html).

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areas are negative in between trill elements (figure 5h), implying that the syrinx is closed.

5.2. In silico experiments with control parameters

With our model, we can systematically switch on and off the control parameters transmural pressure $p_t$ and TL activity to determine how they affect amplitude modulations and frequency modulations. Figure 6 shows what happens when we deactivate the TL muscle, the transmural pressure modulation and both. First, we observe that turning off the transmural pressure has a very small effect on either the onset of sound elements, AM or FM (compare figure 6b,c). Also during the fast trills, both AM and FM closely resemble the original coo recording in figure 6a. However, switching off the TL has profound effects on both gating and FM (figure 6d,e), compared with the original recording. Obviously there is no distinct gating of sound elements anymore. However, the overall amplitude of the sound is still modulated, but now by the bronchial pressure. The remaining small depth of FM is the result of changes in transmural pressure. By turning off both the TL and the transmural pressure as modulators of $Q$ (figure 6f), practically no FM remains and the amplitude is modulated by the bronchial pressure.

5.3. Asymmetry between expiration and inspiration

In a typical ring dove coo, nonlinear transitions such as period doublings and chaos are rare during expiration, and the radiated output signal is almost purely tonal. The amplitude of the harmonics $2 \times f_0$ and $3 \times f_0$ during a steady part of the second syllable for the coo depicted in figure 3a measures $-55$ and $-40$ dB, respectively, compared with $f_0$. These values are very similar to published values: both $2 \times f_0$ and $3 \times f_0$ are 40 dB lower in amplitude, respectively, in Ricle et al. (2004) and 40 and 45 dB lower in Beickers et al. (2003b). The inspiratory note following expiration, on the other hand, is characterized by richer harmonic spectra (figure 3a). The amplitude of the harmonics $2 \times f_0$ and $3 \times f_0$ are 8 and 12 dB higher compared with the fundamental frequency.

Our model also exhibits more rich harmonic spectra during inspiration than during expiration (figure 7). The first and second harmonic measure, respectively, $-22$ and $-34$ dB in amplitude compared with the fundamental during expiration, and $-6$ and $-12$ dB during inspiration. These results imply that the geometry of the model can influence the harmonic sound spectra, because the shape of the LVM differs between simulated expiration and inspiration.

6. DISCUSSION

We establish a novel biomechanical framework for sound production in ring doves (S. risoria). Integrating published experimental data, we hypothesize that (i) the TL modulates the position of the LVM and as such the syringeal aperture and (ii) both TL stress and the transmural pressure affect tension in the LVM. We designed and implemented a quantitative biomechanical model to confirm the validity of these hypotheses. Our simple nonlinear model reproduces the coo with great accuracy and as such provides strong evidence for our biomechanical framework. This is not a trivial result, because nonlinear dynamical systems make the principle of superposition no longer applicable: different excitations may result in different time courses, described by nonlinear dynamics theory (Arrowsmith & Place 1990; Titze et al. 1993; Strogatz 1994). In steady-state simulations with a previous version of our model, we showed that different parameter values can lead to distinct oscillation patterns, and small perturbations induced jumps from one attractor to the other (Zaccarelli et al. 2006). In principle, the interplay of forces that affect rest areas, stiffness and subyngueal pressure can lead to nonlinear phenomena, such as subharmonics, biphonation or deterministic chaos (Fitch et al. 1998; Wilden et al. 1998; Fitch et al. 2002). In a typical ring dove coo, register transitions to aphony, period doublings or chaos are rare during expiration or inspiration. The simulations with physiological input parameters also (figures 5 and 6) do not exhibit transitions to different dynamical regimes. Ring dove coos can also exhibit punctuated frequency jumps (Beickers et al. 2003a), but these are not reproduced by our model.

We present the first model of bird sound that implements a muscle model to calculate force produced by the muscle. The force production by the muscle is based on its actual contractile properties and activation and not simply a function of EMG activity.

Larsen & Goller (1999) observed 0.5–1.0 mm oscillations of the LVM in pigeons. We can derive the maximal oscillation amplitude of one modelled LVM from figure 5d, using equation (4.7). We have to consider mass 2, because Larsen & Goller (1999) had a top view of the syrinx. The maximal oscillation amplitude of our modelled LVM is 0.8 mm (4.8/2X3.0), which corresponds very well with the observed 0.5–1.0 mm. Larsen & Goller (1999) also suggest that a smaller amplitude vibration (0.001–0.1 mm) exists on top of the 0.5–1.0 mm oscillation using a vibration detector that detected light reflectance of the LVM. This signal is hard to interpret in terms of lateral movement of the LVM and could, for example, also represent an oscillation in dorsoventral closure or a tracheal wall vibration. We do not observe this small amplitude oscillation in our simulations.

The thickness (width) of the LVM is 2- to 16-fold higher than reported in other species. In the closely related rock pigeon (C. livia), the LVMs are masses of connective tissue measuring up to 0.1 mm thick (Goller & Larsen 1997). In ducks, reported values range from 360 (Frank et al. 2006) to 750 $\mu$m (Warner 1972). The LVMs in ring doves seem to more closely resemble the consistency and geometry of the mammalian vocal folds or songbird’s labia. Until direct observations were made in situ of the oscillating LVMs by Goller & Larsen (1997), the medial tympaniform membranes were thought to be the vibrating sound sources. These
much thinner membranes (5–20 μm; Casey & Gaunt 1985) inspired the implementation of quantitative models where the sources were modelled as a membrane (Fletcher 1988) or string (Casey & Gaunt 1985). Our model provides a better description of the actual syrinx geometry.

6.1. Harmonics in bird song

The membrane- and string-based mathematical models were initially also implemented because they provided a mechanical basis to explain the almost pure-tone sounds generated by many birds (Casey & Gaunt 1985; Fletcher 1988, 1989). However, sound seems to be predominantly made by colliding syringeal labia (songbirds; Larsen & Goller 2002) or LVMs (Goller & Larsen 1997) just as in humans, other mammals or geckos (Paulsen 1967). As such, the syrinx produces a harmonically rich signal. Recent papers provide an explanation how many birds reduce the higher harmonics and radiate their typical, almost pure-tone sounds. The upper vocal tract acts as a filter in ring doves (Beckers et al. 2003b) and is actively tuned to enhance the fundamental frequency of song during vocalization in some songbirds (Riede et al. 2006) and doves (Riede et al. 2004; Fletcher et al. 2005).

Our model suggests that the geometry and rest position of the syrinx can also influence the harmonic spectra drastically (figure 7). Simulations with constant rest areas demonstrate collision-free oscillations even at high pressures (3.0 kPa = 30 cmH2O), mainly because the pressure acts only on the first mass via the lower plate. This leads to an oscillation pattern characterized by weak harmonics compared with standard two-mass models, where avoidance of collisions can be obtained only at pressure values slightly above the onset pressure. During the coo simulation, the syrinx is in a persistent convergent shape (a1/a2 > 1, figure 4a). As

Figure 6. The effect of control parameters on the trill. (a) Recorded sound in vivo. (b–e) Model simulations with (c) no transmural pressure, (d) no TL activity and (e) no transmural pressure and no TL activity. In (e), the rest areas are constant (0.3 mm²). In (d), Q(t) = 1 (see equation (4.9)) and rest areas are constant (0.3 mm²). Superimposed on spectrograms are: blue line, f0 analysis of recorded coo in (a); yellow–red line, f0 analysis of current signal. (a(i)–e(i)) sound spectrograms, (a(ii)–e(ii)) sound oscillograms.
such, the suprasyringeal pressure has little effect on the masses, which might lead to reduced source–tract interaction. This again suggests that filter mechanisms in doves are closer to those in human phonation (Beckers et al. 2003b) in contrast to other possible explanations, such as the soprano model.

### 6.2. Control of sound production

We can conclude that the complex interplay of bronchial pressure, syringeal muscle force generation and transmural pressure all affect precise amplitude and frequency control. In the case of ring doves, the syringeal muscles have the most profound effect on both AM and FM. Nevertheless, a separated physiological correlate with amplitude or fundamental frequency of the produced sound (Gaunt et al. 1982; Beckers et al. 2003a) seems not to be the case. Even bronchial pressure directly affects the fundamental frequency (figure 6d,e). The implementation of a muscle model to calculate force produced by the muscle, instead of EMG correlates, provides an explanation for the fast frequency rise and fall at the on- and offset of each trill element.

Our model suggests that the control of FM during sound production is relatively independent of a pressure difference between air sacs compared with direct muscular control in ring doves. Brackenbury (1972) shows that a small caudocranial pressure gradient exists in the air sac system. This gradient plays an important role for the gas exchange during ventilation. He provides the only direct measurements of differential pressure between air sacs to our knowledge, and demonstrates that the difference between the ICAS and anterior thoracic air sac is negligible, and that the difference between the ICAS and abdominal air sac is only one-tenth of the parent pressure. During clucking in a chicken the maximal pressure in the ICAS is 1.0 kPa (equal to 10 cmH₂O), while the differential with the anterior thoracic air sac maximally measures only 0.03 kPa (Brackenbury 1972). Furthermore, the transmural pressure is very small compared with the pressure that can be exerted on the LVM by the TL muscle (1.0 versus 20 kPa).

Our *in silico* experiments have their *in vivo* experimental counterparts and thus lead to testable predictions. Switching off the TL as in figure 6 equals performing a bilateral nerve cut experiment. Switching off the transmural pressure equals an experiment where the ICAS syringeal pressure is levelled, e.g. by making a hole in the bronchus. Therefore, we expect that a coo after a bilateral nerve cut exhibits similarity to figure 6d. Levelling the bronchial and ICAS pressure might be a more difficult experiment, because the structural integrity of the syrinx is easily affected.

The small FM range of 400 Hz in ring doves is limited, but might still play an important role in perception (Beckers et al. 2001). For human listeners, an illustrative example is the two-tone vocalization of the common cuckoo (*Cuculus canorus*): the two tones are distinct, but their fundamental frequency (650 and 550 Hz, respectively) differs by only 100 Hz. Although many non-oscine’s vocalizations may have a limited frequency range, almost every family harbours species capable of considerable FM sweeps or intricate song (Ficken et al. 2000). For example, FM ranges 1–3 kHz in the northern lapwing (*Vanellus vanellus, Charadriidae*) and the oystercatcher (*Haematopus ostralegus*), 1–7 kHz in the American woodcock (*Scolopax minor*), 4–9 kHz in juvenile tawny owls (*Strix aluco, Strigidae*), 2.5–9 kHz in the woodcock (*Scolopax rusticola, Scolopacidae*) and even 1.5–9 kHz in the common shelduck (*Tadorna tadorna, Anatidae*; Bergman & Helb 1982; Kroodsma 2005).

The classification of the songbirds and the mechanisms explaining the radiation of the group into the most diverse and numerically dominant avian order are still under debate (Ericson et al. 2003; Barker et al. 2004). Among other hypotheses, the evolution of a complex syrinx and the ability of vocal learning have been suggested and discussed to contribute to this radiation (e.g. Raikow 1986; Baptista & Trail 1992). The songbird syrinx design is highly conserved in evolution (Ames 1971; King 1989) and has six to eight pairs of muscles (King 1989).

However, there seems to be no correlation between syringeal and song complexity (Gaunt 1983; Baptista & Trail 1992). Some syringeal muscles have been correlated with fundamental frequency or amplitude of sound (Goller & Suthers 1996a,b; Suthers et al. 1999), but the biomechanical effects of each individual muscle, let alone potential combinations of differently recruited muscles, e.g. muscle synergies (d’Avella & Bizzi 2005; d’Avella et al. 2003, 2006), are far from understood. Our model suggests that independent control of song characteristics is not possible with the simple syringeal morphology of the ring dove, as suggested before by Gaunt (1983). We speculate that songbirds evolved a syrinx design that allowed for the independent control of sound parameters. Uncoupling the control of different sound parameters as
an evolutionary key innovation would lead to a tremendous increase in the possible variation of song, which provides an additional explanation for the rapid diversification and speciation of songbirds.

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