Elasto-capillarity in insect fibrillar adhesion

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The manipulation of microscopic objects is challenging because of high adhesion forces, which render macroscopic gripping strategies unsuitable. Adhesive footpads of climbing insects could reveal principles relevant for micro-grippers, as they are able to attach and detach rapidly during locomotion. However, the underlying mechanisms are still not fully understood. In this work, we characterize the geometry and contact formation of the adhesive setae of dock beetles (Gastrophysa viridula) by interference reflection microscopy. We compare our experimental results to the model of an elastic beam loaded with capillary forces. Fitting the model to experimental data yielded not only estimates for seta adhesion and compliance in agreement with previous direct measurements, but also previously unknown parameters such as the volume of the fluid meniscus and the bending stiffness of the tip. In addition to confirming the primary role of surface tension for insect adhesion, our investigation reveals marked differences in geometry and compliance between the three main kinds of seta tips in leaf beetles.

1. Introduction

The miniaturization of engineered components in industrial processes is challenging, not only because of the need to maintain high efficiency or functionality, but also because of the physical constraints on their manipulation. At the scale where stiction and surface tension dominate other forces, how do we devise an efficient tool that reliably grabs and releases small and fragile objects? One strategy is to control and to take advantage of these surface forces [1–3]. In nature, such a solution has evolved in a number of organisms efficiently employing adhesion at the micrometre scale.

There are two main types of adhesive mechanism in climbing animals: ‘dry’ adhesion (as found in geckos) and ‘wet’ adhesion (used by insects, spiders and tree frogs). Dry adhesion in geckos relies on compliant setae and nanometric spatulae that adhere by van der Waals forces and has been studied extensively [4]; several gecko-inspired fibrillar adhesives have already been designed and tested [5,6]. By contrast, wet adhesion relies on the presence of small amounts of liquid secreted by the animal and the resulting viscous and capillary forces. Wet adhesion occurs in animals bearing two different types of adhesive structures, ‘smooth’ and ‘hairy’ pads [7]. Smooth pads (e.g. in stick insects, cockroaches and bees) are soft ‘cushions’ forming one single liquid bridge with the substrate. Hairy pads (e.g. in beetles and flies) are structures covered with dense arrays of slender adhesive setae (figure 1b,c), each of which forms a liquid bridge when it touches the substrate.

Although hairy pads are promising for bioinspired applications, the small size of individual setae makes direct observations challenging. Each seta tip is only a few micrometres wide and only few studies have attempted to design elaborate strategies to measure in vivo their mechanical and adhesive properties [8–11]. Nanoindentation measurements on the setae of lady beetle Coccinella septempunctata revealed a large difference in Young’s modulus...
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[21,23], but decreased it on rough surfaces [20]. Dry contact
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rejected on the grounds that a meniscus of Newtonian
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strong attachment and detachment during locomotion.

between the tip (1.2 MPa) and the stalk (6.8 GPa) [12]. These
values are consistent with the ability of Gastrophysa viridula
seta tips to accommodate surface roughness [13]. On the
other hand, the volume of liquid in the capillary fluid bridges
is so far unknown, although it is thought to be smaller than a
few femtolitres [14]. Some other interesting morphological
characteristics of the setae are still not fully understood: the
shape of the seta tips varies both between insect species,
and between different pad areas on the same foot [15,16].
In leaf beetles (figure 1), one can identify three main tip geo-
metries: spatula-shaped, discoidal and pointed. Although the
detailed function of each tip geometry is still unclear, first
measurements [8] showed that discoidal tips produce larger
adhesion forces than other tips. In addition, they were
found to have a larger spring constant. As discoidal setae
are only found in males, they may play an important role
in the mating behaviour of the beetles [16]. By contrast,
spatula-shaped tips showed a stronger direction-dependence
and are probably specialized for the rapid switching between
strong attachment and detachment during locomotion.

The existing models for fibrillar adhesion suffer from a
lack of reliable experimental information at the scale of individ-
ual setae. A simple capillary bridge model has been
rejected on the grounds that a meniscus of Newtonian
liquid cannot explain the high shear forces of insect pads
[17–20], as well as their weak velocity-dependence in the
case of smooth pads [21]. Therefore, many theoretical
descriptions of insect adhesion are based on dry contact
[21,22]. As a result, the possible advantages of an intervening
liquid are not considered. Experiments on smooth adhesive
pads in insects have shown that reducing the volume of
adhesive fluid increased adhesion on smooth substrates
[21,23], but decreased it on rough surfaces [20]. Dry contact
indeed fails to provide significant adhesion as soon as the
distance between both solids exceeds a few tens of nano-
metres. Although the storage of elastic energy has been
pointed out as a possible mechanism helping rapid detach-
ment in gecko dry adhesion [4], this factor is ignored in
many adhesion models and its detailed interplay with capil-
ary forces has not been described. Theoretical work on the
interplay between flexible structures and capillary forces
exists (e.g. [24,25]), but it has not yet been applied to the
field of insect adhesion.

The primary goal of this work is to characterize and better
understand the interaction between adhesive setae of the dock
beetle G. viridula and capillary forces during contact with a
substrate. We focus on the elastic properties of the seta tip
and the volume of liquid in the capillary meniscus, thereby
comparing the three main types of seta tip in leaf beetles
discoidal, spatula-shaped and pointed). Our approach
combines experimental and theoretical work. First, the three-
dimensional geometry of seta tips in contact with glass is
obtained in vivo using interference reflection microscopy
(IRM) [18]. The experimental set-up and results are described
in §§2 and 3, respectively. Second, we develop a simplified
beam model of a seta tip loaded by capillary forces (§4). The
unknown parameters of the model (namely the stiffness of
the beam and the volume of liquid in the meniscus) are then
determined by matching the predicted geometry to the exper-
imental data (§5). Further predictions of the model, including
adhesion force levels, are discussed in §6.

2. Experimental set-up

The mechanical properties of insect cuticle greatly depend on
its degree of hydration [26], and it is probably that hydration
also affects insect adhesive setae. It is therefore important to
work with living insects. We studied male dock beetles
(G. viridula; n = 5). For each of beetle, we analysed the behav-
iour of 10–14 setae of each type (spatula-shaped, discoidal or
pointed tip—figure 1d–f) from the most distal seta-bearing
(third) tarsomere of the rear or middle leg, resulting in a
total of n = 60 for each kind of seta tip.

Using IRM (figure 2), we imaged the contact geometry of
the seta tips. The beetles were immobilized by embedding
them on their back in Blu-Tack (Bostik) and Parafilm
(Bemis) tape mounted on a metal rod; Blu-Tack was also
used to isolate one of the legs. Its tarsus was fixed on the

Figure 1. The leaf beetle Gastrophysa viridula and the morphology of its
adhesive pads, (a) macroscopic view (ruler divisions are 0.5 mm), (b) ventral
view of the tarsus and (c) setae. (d–f) The three main types of setae studied
in this paper: spatula-shaped (d), discoidal (e) and pointed (f).

Figure 2. Experimental set-up: a male beetle (1) is attached to a piezo stage
(2) and one of its legs is brought into contact with a glass coverslip (4).
Monochromatic epil-illumination (3) reveals interference fringes that result
from the thin air gap between the tip and the glass. We measured both
the geometry of the contact zone (total length Lw and width profile w(β))
as well as the tip angle αw as calculated from the first fringes. (Online
version in colour.)
dorsal side with vinyl polysiloxane impression material (Elite HD + light body, Zhermack, Badia Polesine, Italy). The last tarsal segment and the claws were bent over and fixed in the Blu-Tack to expose the distal pad on the third tarsal segment and to prevent the claws from touching the surface. The holder with the beetle was attached to a closed-loop piezo stage (P-611 ZS, Physik Instrumente) that moved in the vertical direction with a resolution of 2 nm. The distal adhesive pad was brought into contact with a glass coverslip mounted under a Leica DMR-HC upright microscope with a 100×/1.25 oil objective. We used switchable bandpass interference filters in the epi-illumination path to achieve monochromatic epi-illumination by isolating the 546 or 436 nm lines from the spectrum of a 100 W mercury arc lamp. We recorded a succession of images for different z-positions on a QIC-FM12 12-bit monochrome camera (QICAM) with an optical resolution comprised between 210 and 270 nm. Figure 3 shows a typical IRM image of the seta tips. It can be seen that the hairs make different levels of contact. The fringe pattern on the proximal (stalk) side of each contact zone represents the part of the seta that is sufficiently close to the substrate so that the air gap between the seta and the glass surface produces interference.

A flexible cantilever beam in wet contact with a substrate can be in different regimes of elasto-capillary equilibrium [24], depending on how much it is deformed by the capillary forces. At high stiffness, the beam does not significantly deform and does not touch the substrate. The liquid forms a capillary bridge that links both structures. At low stiffness, the tip of the beam touches the substrate and the meniscus takes the shape of a liquid wedge (figure 2, right). Our experimental observations suggest that the latter regime describes the behaviour of the very thin and compliant seta tips. Recent cryo-SEM images of fly setae [27] also confirm this conclusion, as most of the liquid was found near the proximal edge of the seta contact zones.

Between each movement of the piezo stage and the subsequent image, sufficient time (3–5 s) was left for the liquid bridge to reach a static equilibrium. This condition is fulfilled when the viscous forces induced by a motion of the liquid bridge are negligible compared to capillary forces. The capillary number $C_a = \mu v / \gamma$ estimates the ratio of viscous to capillary forces associated with a Poiseuille flow between two parallel plates [25], where $\mu$, $\gamma$ and $v$ are the dynamic viscosity, the surface tension and the characteristic velocity of the movement. If considering a vertical recirculation of the fluid, the associated capillary number $C_a$ scales as $C_a L^2 / h^2$ with $L$ the characteristic length of the horizontal flow and $h$ the distance between the plates. Previous work estimated the liquid viscosity to be $\mu \approx 10^{-3}$ Pa s [11]. The surface tension of most oil-based liquids is approximately $\gamma \approx 20$ mN m$^{-1}$ [28]. Finally, our images revealed that $v$ was of the order of 0.1 nm s$^{-1}$, so the corresponding capillary number $C_a \approx 5 \times 10^{-7}$ is indeed much smaller than unity. $C_a$ also conforms to this criterion as long as $h > 10$ nm, a distance where van der Waals forces between both plates must be taken into account and continuous fluid mechanics is not applicable anymore.

During our measurements, we sometimes observed small back-and-forth movements of the seta tips (of approx. 1 µm) which may be induced by fluctuations in the haemolymph pressure or muscle contractions. Thus, the uncertainty about the actual z-position of the setae was much larger than the nanometre resolution of the piezo stage, thereby increasing the variability of our results.

### 3. Experimental results

We first analysed the shape of the contact area of 45 seta tips (15 of each kind). The width $w$ at any given distance $s$ from the distal end of the tip was approximated by linear, lemniscate and parabolic functions corresponding to spatula-shaped, discoidal and pointed tips, respectively (figure 4a). The corresponding dimensionless equations $\tilde{w}(s)$ are given in table 1. Average values were calculated for the maximum width $w_M$ and length $s_c$ of the full contact area. The length $s_c$ was defined as the transition from the seta tip to the seta stalk. In the following, $w_M$ will be used to normalize lengths and distances ($\tilde{w}$, $s$).

Even though the flexible seta tip extremities should be very close to the substrate, there is no visible transition from dry to wet contact on the IRM images. The image contrast is reduced by stray light reflected from the dorsal side of the seta tip but some liquid may also be trapped between the seta tip and the substrate. Nevertheless, if this layer is thin enough, both normal and tangential forces can be transmitted from the seta to the substrate just like for a dry contact (although with a different friction coefficient). No interference is observed in the wet region: stray light from the dorsal side of the seta tip and the high brightness of the background conceal the light interferences produced by two surfaces of similar refractive indices (glass substrate, $n_g \approx 1.52$, and insect secretion, $n_w \approx 1.47$ [29]). On the other hand, the liquid–air interface is present right before the first bright interference fringe. The proximal–distal length of the wet contact zone $L_w$ (i.e. the distance between this interface and the seta tip, along the medial symmetry axis of the seta contact zone, figure 4b) was measured for each z-position of the piezo stage (figure 2).

The angle $\alpha(s)$ is defined as the local inclination of the seta at a curvilinear distance $s$ from the end of the tip. Outside of the wet contact zone, $\alpha(s)$ can be estimated from the spacing between interference fringes. Of particular interest is the angle $\alpha_w$ (at abscissa $s_w$, i.e. the liquid–air interface), which is deduced from the distance between the first two
bright fringes adjacent to the meniscus. Classical theories for thin films assume that interference occurs between light rays reflected from two almost parallel interfaces, i.e. for very small $\alpha(s)$. Because this approximation is not valid in our case, we had to reconstruct the interference profile by ray tracing, according to the general theory developed by Wiegand et al. [30]. Our calculations are therefore valid also for larger $\alpha(s)$ and they take into account the finite aperture of illumination. Finally, we measured the average angle change along the fringe profile $\tilde{a}$ (the dot represents derivation with respect to the curvilinear abscissa $s$) for each tip and each contact step. Fringes are not always straight lines perfectly perpendicular to the longitudinal direction of the tip (defined in figure 4b), so the distance between them is subject to a significant measurement error (typically 2 pixels here, corresponding to 114.6 nm), which translates into uncertainty regarding $\alpha_w$. Similarly, a maximal error of 5 pixels was estimated for the positioning of the fluid–air interface and hence $L_w$ (cf. characteristic error bars in figures 5 and 6). The local measurement of $\alpha(s)$ for each position of the stage $z$ provides an approximate reconstruction of the three-dimensional geometry of the seta tip (figure 4c). However, only the local slope is measured; the absolute distance to the substrate as well as the fluid wedge length and height are unknown (see the discontinuity of the profiles in figure 4c).

Figure 5 shows the seta contact length $L_w$ as a function of the piezo stage displacement $z$ (the first contact of the tip with the substrate corresponds to $z = 0$). The three kinds of tips are clearly differentiated: the slope is about four-times higher for discoidal tips than for the spatula-shaped and pointed tips. The contact length $L_w$ also saturates at $s_c$ for both discoidal and spatula tips, thus presenting a defined maximum tip length unlike pointed tips. For each of the three seta types, a significant difference was observed between contact length at the same $z$-position during loading (increasing $z$) and unloading (decreasing $z$). This phenomenon is typical of adhesive contacts [31]. However, the hysteresis is not visible when the local slope $\alpha_w$ at the fluid–air interface is plotted against the contact length $L_w$ (figure 6). This suggests that the hysteresis could be attributed to either backlash in the insect fixation, uncontrolled movement of the insect (62) or partial bending of the stalk, each of them possibly resulting in imperfect transmission of the vertical movement from the stage to the seta tip. The absence of significant hysteresis indicates that the tip is always in a local equilibrium that does not depend on whether the seta is attaching to or detaching from the substrate. Because friction forces are reversed when switching from loading to unloading (they always oppose the motion), they must not significantly affect this local equilibrium. The observed horizontal sliding of the tips as the piezo stage is moving (distal during loading,
4. Elasto-capillary model of the seta tip

Each seta tip can be modelled as a thin flexible beam clamped at one end, corresponding to the transition to the seta stalk (figure 9). When the pad is not in contact with the substrate, the seta tips are assumed to be straight and tilted with an angle $\alpha$. When the beam touches the substrate, it bends in response to two forces: (i) the reaction force $N_d$ from the solid–solid contact and (ii) the surface tension forces from the capillary meniscus. This meniscus can be approximated by a liquid wedge of volume $V$ between the beam and the substrate. The corresponding loads include the Laplace pressure $\gamma/R$ inside the meniscus and the capillary force $\gamma w$ along the contact line, where $\gamma$, $R$ and $w$ are the surface tension, the radius of curvature of the meniscus and the width of the tip at the proximal edge of the meniscus, respectively.

4.1. Geometry parameters

Seta tips are a few hundred nanometres thick [32], so their aspect ratio (thickness over length) is smaller than 0.1. They can thus be considered as slender beams which undergo significant deflection while the corresponding strain remains small. We define the curvilinear coordinate $s$ along the neutral axis of the beam, with the origin $s_0 = 0$ at the very tip. Indices $a$, $d$, $w$ and $c$ correspond to the extremity of the beam, the end of the solid–solid contact area, the end of the fluid-mediated contact area (fluid–air interface) and the clamping point, respectively. The beam deflection is expressed by a parametric equation $[x(s), z(s)]$, where $z$ is the distance to the substrate and $x$ is the distance to the beam extremity, parallel to the substrate. The parametrization is such that

$$\frac{dx}{ds} = \cos \alpha(s)$$

and

$$\frac{dz}{ds} = \sin \alpha(s),$$

where $\alpha(s)$ is the local slope of the beam. It is obtained by solving Euler–Bernouilli’s equation

$$\frac{d\alpha}{ds} = \frac{M(s)}{B(s)}$$

where $d\alpha/ds$, $M(s)$ and $B(s)$ are the curvature, the local bending moment and the local bending stiffness of the beam, respectively.

The bending stiffness $B(s)$ is related both to the width $w(s)$ and the height $h(s)$ of the cross-section of the seta tip. As shown in §3, the width profile has been measured from the IRM images and averaged. It is normalized by its maximum width $w_M$ and approximated with the function $\tilde{w}(\tilde{s})$, where $\tilde{s} = s/w_M$ (table 1). On the contrary, the local thickness $h_s$ is not directly accessible with our experimental set-up. Einmüller et al. reported thickness measurements of spatula tips made by X-ray microscopy; it varies from about 100 nm to about 500 nm in the first 5 µm from the tip [32]. This increase is well approximated by a square-root function:

$$\frac{h(s)}{h_M} = \sqrt{\frac{1}{25} + \frac{24s}{25w_M}},$$

with $h_M = 500$ nm the thickness at $w(s) = w_M$. The local Young’s modulus is also unknown. Transmission electron...
microscopy [32] has revealed that the tips are not homogeneous structures. They rather consist of a solid hull filled with fibrillar material. The dorsal and ventral cuticles could thus be the main contributor to the bending stiffness (similar to an I-beam). Assuming a hull of constant thickness, the bending stiffness is proportional to the square of the total beam thickness:

$$B_1(s) = B_M \frac{w(s)}{w_M} \left( \frac{h(s)}{h_M} \right)^2. \quad (4.5)$$

This expression is based on a succession of hypotheses a priori only justified for spatula tips. As no similar measurements are available concerning discoidal or pointed tips, we choose to additionally consider a simpler profile of constant thickness and homogeneous Young’s modulus:

$$B_2(s) = B_M \frac{w(s)}{w_M}, \quad (4.6)$$

where $B_M$ now represents the maximum bending stiffness. Both profiles were examined for each tip geometry.

4.2. Loads and bending equations

Shear stresses induced by bending are safely neglected as soon as the beam is sufficiently slender. By contrast, substrate roughness induces significant stretching, which can strongly modify the mechanical behaviour of the seta [13]. We here consider the substrate to be perfectly flat: the pure bending of the beam is then described by equation (4.3). Boundary conditions associated with equations (4.1)–(4.3) are defined at the transition from solid–solid to liquid-mediated contact $s = s_d$:

$$x(s_d) = x_d, \quad (4.7)$$

$$z(s_d) = 0 \quad (4.8)$$

and

$$a(s_d) = 0. \quad (4.9)$$

The loads depend on the geometry of the seta (figure 9). Because the solid–solid contact zone is assumed to be perfectly flat, there is no net moment in this part of the beam. We can then assume that the (unknown) resultant reaction force normal to the substrate $N_d$ is concentrated at the edge of the dry contact zone (position $s_d$). The absence of significant hysteresis in figure 6 suggested that solid friction forces do not strongly modify the elasto-capillary equilibrium. To test this hypothesis, we consider a friction force $T_d = \tau S$ that opposes the sliding motion of the seta, where $\tau$ is the static shear stress and $S = \int_0^s w(s) \, ds$ the area of solid–solid contact. According to figure 9, $\tau$ is positive during loading (distal sliding of the tips) and negative during unloading (proximal sliding). The case $\tau = 0$ was first considered for the calibration of the model on experimental data. Then $\tau$ was varied in order to assess its influence on the elasto-capillary equilibrium.

The adhesive liquid mostly contains lipids [33], and the resulting low contact angle contributes to the robustness of the adhesion mechanism on a broad range of substrates. For the sake of simplicity, we here assume that the liquid perfectly wets both surfaces (zero contact angle). The liquid meniscus is then approximated by a circular arc of radius $R$ tangent to both the beam and the substrate. Surface tension $\gamma$ contributes twice to the beam loads. First it exerts a force per unit width at the contact line (position $s_w$), parallel to the liquid–air interface (i.e. tangent to the beam). The second load is a negative Laplace pressure $\Delta p = -\gamma/R$ uniformly distributed over the wet part of the beam.
Figure 8. Seta inclination $\alpha_w$ at the fluid–air interface plotted against contact length $L_w$; symbols show the average of many measurements over 10 seta tips from the same individual. (a) Spatula-shaped (squares), (b) discoidal (circles) and (c) pointed tips (triangles). Filled symbols represent loading (increasing $z$), and empty symbols unloading (decreasing $z$). Solid, dashed and dotted lines represent fits by the elasto-capillary model for a friction coefficient of $\tau = 0$, $\pm 10$ and $\pm 30$ kPa, respectively. Additional plus and minus symbols indicate the sign of coefficient $\tau$. Thickness profile $B_1$ (equation (4.5)) was used for the fit of discoidal tips, and profile $B_2$ (equation (4.6)) for spatula-shaped and pointed tips. (Online version in colour.)

Figure 9. Elasto-capillary model: a flexible beam (length $s_z$, width $w(s)$) is in contact with a flat substrate (hatched area). It is clamped at one end at a distance $Z_0$ from the substrate and with an inclination angle $\alpha_w$. A portion $s < s_z$ of the beam is in solid–solid contact with the substrate. Another portion $s_z < s < s_w$ is separated from the substrate by a wedge-shaped liquid meniscus of volume $V$. The horizontal distance between the beam tip and the meniscus edge is denoted $L_w$. The loads applied to the beam are the solid–solid contact reaction force $N_c$, the associated friction force $T_c$, surface tension at the contact line $\gamma w_w$ and the Laplace pressure $\gamma/R$, where $R$ is the curvature radius of the meniscus. The resulting efforts at the clamp are $N_c$, $T_c$ and $M_c$. (Online version in colour.)

(s_d < s < s_w). For simplicity, we, furthermore, assume that $w_a \gg R$ so the curvature of the liquid meniscus is much smaller in the $(x, y)$-plane than in the $(x, z)$-plane.

In the wedge region ($s_d < s < s_w$), the resulting local moment in the beam is given by

$$M = N_d (x - x_d) - \pi s_z - \frac{\gamma}{R} I(s),$$

where

$$I(s) = \int_{s_d}^{s} [(x - x(t)) \cos \alpha(t) + (z - z(t)) \sin \alpha(t)] w(t) \, dt$$

and $x, z, \alpha$ and $M$ all depend on position $s$. In the solid–solid contact zone ($s_w < s < s_c$),

$$M = N_d (x - x_d) - \pi s_z - \frac{\gamma}{R} I(s_w) + \frac{\gamma w_w}{2} [(z - z_w) \cos \alpha_w - (x - x_w) \sin \alpha_w].$$

The volume of liquid $V$ in the wedge is computed from the beam shape:

$$V \simeq \int_{s_d}^{s_w} w \cos \alpha \, ds + R^2 w_w \left[ \sin \alpha_w \left( 1 + \cos \alpha_w - \frac{\pi - \alpha_w}{2} \right) \right].$$

Finally, the normal ($N_c$) and tangential ($T_c$) efforts at the clamped end $s_c$ are computed according to

$$N_c = \gamma w_w \sin \alpha_w - N_d + \frac{\gamma}{R} \int_{s_d}^{s_w} w(s') \cos \alpha(s') \, ds'.$$. 


The predictions of our model are summarized in figure 8. Although the model captures well the behaviour of $\varphi_{aw}\left(L_{aw}\right)$ for intermediate values of $L_{aw}$, it fails to compute a valid solution when $L_{aw}$ is either too small or too large. Best values of $(\varphi, \Omega)$ determined for each seta tip are then averaged geometrically for each tip type (table 2). Trial values for $\varphi$ and $\Omega$ are discrete and equidistant on a logarithmic scale: the corresponding standard deviations are thus expressed in exponential form.

The associated dimensionless quantities $B_M$ and $V$ are represented in figure 10. Significant differences are obtained depending of the thickness profile used in the model. The non-homogeneous profile $B_M$ (equation (4.6)) offers more consistent results for the discoidal tips of different individuals. By contrast, $Y$ and $n_v$ criteria speak in favour of profile $B_M$ and liquid volume $V$ are systematically associated with larger amount of fluid is systematically associated with a higher degree of stiffness.

### 5.2. Adhesion force

The resulting force in the direction normal to the substrate $N_c$ represents the adhesion force developed by a single seta. It generally increases with the contact length $L_{aw}$ (figure 11) but also significantly differs from one seta type to the other. For the same contact length, discoidal tips generate adhesion 2–3 times larger than spatula tips and 8–12 times larger than pointed tips. On the other hand, spatula and pointed tips can be seen as more robust than the discoidal ones, as a small change in contact length will not result in a large drop in adhesion force.
Figure 10. Dimensional parameters of the model adjusted on experimental data: bending modulus $B_t$ at the widest point of the tip versus volume of liquid $V$ in the meniscus. Three tip geometries are represented (spatula, squares; discoidal, circles; pointed, triangles) as well as two thickness profiles ($B_1$ (solid lines, filled markers) and $B_2$ (dashed lines, empty markers)). The markers indicate particular solutions fitted for every trial batch and the box delimits an area of one standard deviation around average value. (Online version in colour.)

Figure 11. Normal force $N_k$ at the tip-to-stalk transition versus contact length $L_w$. The three tip geometries are represented (spatula, squares; discoidal, circles; pointed, triangles) as well as the corresponding thickness profiles ($B_1$ (solid lines, filled markers) and $B_2$ (dashed lines, empty markers)).

5.3. Friction force

The consideration of a small non-zero friction force in the analytical model ($\tau = \pm 10$ kPa, dashed lines in figure 8) brings the prediction for spatula-shaped and pointed tips outside of the experimental error bars. The upper (respectively, lower) curve corresponds to negative (respectively, positive) $\tau$. Including friction in this case thus results in a strong differentiation between attachment and detachment that is not observed experimentally. On the other hand, higher values for the shear stress ($\tau = \pm 30$ kPa, dotted lines in figure 8) influence only slightly the behaviour of the model prediction for discoidal tips. We conclude that friction is not a dominant effect for spatula-shaped and pointed tips in this particular configuration where the insect leg is brought in normal contact with a horizontal smooth substrate, but could have a role for discoidal tips.

6. Discussion

Once the parameters $\Phi$ and $\Omega$ are determined, the model provides $\alpha_w(L_m)$ curves in good agreement with the experimental data. Nevertheless, the model sometimes failed to produce a valid solution, mostly at very small or at large $L_m$. Either there is no value of $R$ that holds the required liquid volume $\Omega$ or the local angle of the tip $\alpha(s)$ becomes larger than $\pi/2$. On the other hand, at small $L_m$ the extremity of the tip might not bend significantly in response to capillary forces, which could invalidate our hypothesis of a wedge-shaped liquid meniscus [24]. On the other hand, the angles measured for $L_w(s) \approx L_w$ correspond to the stalk angle, which is not considered in our model. However, these limitations do not undermine the quality of the fit in the intermediate range of $L_m$.

After matching to experimental data, the approximated elasto-capillary number $\Phi$ always gravitates around unity. This dimensionless number represents the ratio between capillary forces and elastic deformation. We then conclude that both ingredients are equally involved in insect adhesion. The match on $\Omega$ yields an estimation of the liquid volume $V$ in a single meniscus. The order of magnitude is tenths of femtolitres, in agreement with the amount of liquid collected from the footprints of a related leaf beetle [11].

The stiffness of each tip inferred in this study can also be compared to other data in the literature. A Young modulus of 1.2 MPa was measured by nanoindentation on the tip of severed setae from the lady beetle $C. septempunctata$ [12]. These results were proven consistent with the deflection of $G. viridula$ seta tips on structured substrates [13]. TEM images revealed that seta tips consist of a fibrillar bulk surrounded by a denser outer shell [32]. The shell is probably stiffer so it would provide most of the resistance to bending, similar to an I-beam. Young’s modulus $E$ of the shell is then given by

$$E \approx \frac{12B}{wh^3 - w(h - 2e)^3} \approx \frac{2B}{ehw^2}, \quad e \ll h,$$  

where $w$, $h$, $e$ and $B$ are the local width and height, the flange thickness and the bending stiffness, respectively. TEM images [32] suggest that $e \approx 125$ nm, whereas the height $h$ can be approximated by profile $B_{1.5}$ (equations (4.5) and (4.6)) and the width $w$ measured from our images (table 1). Our combined experiments and elasto-capillary model provided estimations of $B_M$ (table 2), from which we can infer Young’s modulus for each seta tip: $E_{spat} \in [8; 32]$ MPa, $E_{disc} \in [46; 73]$ MPa, $E_{point} \in [5; 8]$ MPa. Our estimations are thus one or two orders of magnitude higher than the nanoindentation results. The two experiments, however, involve different bending deformations (figure 12). In the present experiment, the seta tip is fully bent and the entire cross-section contributes to the stiffness. By contrast, the nanoindentation experiments [12] were performed with an indentation depth of about 50 nm, which is only sufficient to bend the thin outer shell instead of actually compressing it. In other words, the force/displacement ratio $F/\delta$ measured in nanoindentation corresponds in first approximation to the bending of a thin sheet of thickness $e$, width and length $w$ and Poisson’s ratio $\nu$ clamped at both ends

$$\frac{F}{\delta} = \frac{16E\nu e^3}{w^2(1 - \nu^2)},$$

rather than the compression of a bulk material in Hertzian
contact (as calculated in [12]):

\[ \frac{F}{\delta} = \frac{4E_{\text{Hertz}} \sqrt{R_c \delta}}{3(1 - v^2)}, \tag{6.3} \]

where \( R_c = 10 \text{nm} \) is the indentation tip radius. The ratio between the two estimations of Young’s modulus is

\[ \frac{E_{\text{Bend}}}{E_{\text{Hertz}}} = \frac{w^2 \sqrt{R_c \delta}}{12r^3} \approx 24. \tag{6.4} \]

Thus, an approximated value of Young’s modulus of the shell by nanoindentation would be \( \approx 29 \text{ MPa} \), which is now of the same order of magnitude as our estimations. Although this approach offers a first understanding of the modulus difference, a more precise comparison could consider other sources of discrepancy, such as the occurrence of finite size effects during indentation.

In vivo compression of \( G. \) viridula setae [8] have already revealed that each of the three kinds of tips has a different spring constant \( k \) (defined as the ratio between a force applied at the end of the tip and its maximum deflection). Discoidal tips \( (k_{\text{disc}} = 0.693 \pm 0.111 \text{N m}^{-1}) \) are significantly stiffer than spatula \( (k_{\text{spat}} = 0.364 \pm 0.039 \text{N m}^{-1}) \) and pointed tips \( (k_{\text{point}} = 0.192 \pm 0.044 \text{N m}^{-1}) \). We can also infer spring constants from our estimations of \( E \) (table 2) by solving equation (4.3) in the limit of small deformation. We obtain \( k_{\text{disc}} \in [0.021; 0.033] \text{N m}^{-1}, k_{\text{spat}} \in [0.033; 0.012] \text{N m}^{-1} \) and \( k_{\text{point}} \in [5.3; 3.4] \times 10^{-4} \text{N m}^{-1} \). Although the same hierarchy appears, the stiffness levels are significantly lower here than in [8]. This can again be understood from the difference in loading between both experiments: in [8], the entire seta is subject to bending with a stalk several orders of magnitude stiffer than the tip. During contact, most of the elastic deformation will thus occur in the tip as described in our model.

Direct measurement of the adhesion force \( N_c \) associated with each seta type is also available from [8]: \( N_{c_{\text{disc}}} = 919 \pm 104 \text{nN}, N_{c_{\text{spat}}} = 582 \pm 59 \text{nN} \) and \( N_{c_{\text{point}}} = 127 \pm 19 \text{nN} \). Once again, our estimations are in fair agreement: they have the same order of magnitude and the ratio between different tips is also consistent, although our model systematically underestimates \( N_c \) by a factor of two. Nevertheless, we get to the conclusion that stiffer hairs lead to higher adhesion. This result is consistent with the idea that a stiffer pad can distribute stresses over a larger area and thereby maximize adhesion [35,36]. The higher adhesion developed by discoidal hairs on smooth surfaces is to be related to their presence on male individuals only. They are indeed expected to enhance attachment to the female elytra during mating. On the other hand, despite granting lower levels of adhesion, the spatula-shaped hairs certainly offer a more robust locomotion strategy, because a small decrease in contact length does not result in a drastic change in adhesion force: when walking on uneven surfaces, sufficient adhesion will be granted even if the pad is not perfectly aligned and tips are in partial contact. For locomotion, perhaps the most essential parameter is the controllability (shear-sensitivity) of adhesion, and it seems that this is achieved most efficiently in the spatula-shaped hairs, as they are highly direction-dependent. The pointed hairs generally achieve only very little adhesion, and may be most important for generating friction by making side-contacts [8].

As described by the analytical model, any flexible structure coupled with a capillary bridge enables generation of adhesion similar to insects with hairy pads. The degree of stiffness allocated to the structure and the amount of liquid used would determine whether strong or robust adhesion is favoured. Such an elasto-capillary equilibrium can also be modified by varying clamping parameters, thus allowing control over adhesion. Further study of the model is necessary for a complete understanding of the elasto-capillary system but will be of great interest for the design of a bioinspired manipulation tool.

7. Conclusion

Many insect species can adhere to smooth substrates thanks to hairy adhesive pads. Although liquid footprints have been observed, the exact amount and the detailed role played by the liquid in the adhesion mechanism were still unclear, as was the function of different kinds of seta tips with different geometry and elastic properties.

In this paper, we have presented IRM measurements of the three-dimensional geometry of the seta tips of a living insect leg in controlled contact with a smooth substrate. Three kinds of seta tips (spatula-shaped, discoidal and pointed) could be distinguished, from both the shape of the contact area and from the average angle between the seta tip and the substrate. This angle was found to be the same for a given contact length, independent of the direction of motion (loading versus unloading).

This observation suggests that there is a local force equilibrium, in which the seta tip is deflected by the normal reaction force from the substrate and the capillary forces from the intervening liquid wedge. We modelled the seta tip as a slender beam and calculated its deflection as a function of both its bending stiffness and the liquid volume. We could then infer these two unknown properties by matching the predicted deflection to the IRM measurements. The model captured well the evolution of the tip geometry with increasing contact area. Moreover, the resulting adhesion force level and bending stiffness correspond to the values obtained by other experimental methods in previous studies. This agreement shows that a simplified model based on the combination of capillary forces and elastic deformations can account for the measured behaviour of seta tips. The observed elasto-capillary number \( \Phi \) of the order of unity.
suggests that both capillary and elastic forces are equally essential to rationalize the adhesion mechanism.

At every step of this study, significant differences were observed between spatula-shaped, discoidal and pointed tips. Discoidal tips are stiffer while pointed tips are more compliant. Discoidal tips also involve a significantly larger volume of liquid. These features are consistent with the biological function of discoidal tips in males during mating.

Surface tension dominates the microscopic realm, and in many different contexts insects have been witnessed to make the most of it [37–40]. This work confirms that the interplay of capillary and elastic forces is probably the key ingredient responsible for the reversible adhesion of hairy pads on smooth substrates. Nevertheless, direct in vivo observation at the sub-micrometre scale of seta tips remains technically challenging, and future work is still required to elucidate and model the mechanics of these remarkable adhesive microstructures.

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References


5. Santos D, Spenko M, Parness A, Kim S, Cutkosky M. 2006 Why are so many adhesive pads on smooth substrates. Nevertheless, direct in vivo observation at the sub-micrometre scale of seta tips remains technically challenging, and future work is still required to elucidate and model the mechanics of these remarkable adhesive microstructures.


